Fractals have been very successful in quantifying the visual complexity exhibited by many natural patterns, and have captured the imagination of scientists and artists alike. Our research has shown that the poured patterns of the American abstract painter Jackson Pollock are also fractal. This discovery raises an intriguing possibility – are the visual characteristics of fractals responsible for the long-term appeal of Pollock’s work? To address this question, we have conducted 10 years of scientific investigation of human response to fractals and here we present, for the first time, a review of this research that examines the inter-relationship between the various results. The investigations include eye tracking, visual preference, skin conductance, and EEG measurement techniques. We discuss the artistic implications of the positive perceptual and physiological responses to fractal patterns.

**Keywords:** fractals, esthetics, visual preference, eye tracking, EEG

### Poured Complexity

The art world changed forever in 1945, the year that Jackson Pollock moved from downtown Manhattan to the countryside of Long Island, New York. Friends recall the many hours that Pollock spent on the back porch of his new house, staring out at the scenery as if assimilating the natural shapes surrounding him (see Figure on the back porch of his new house, staring out at the scenery as moved from downtown Manhattan to the countryside of Long Island). The art world changed forever in 1945, the year that Jackson Pollock

One issue agreed upon early in the Pollock story was that his paintings represent one extreme of the spectrum of abstract art, with the paintings of his contemporary, Piet Mondrian, representing the other. Mondrian’s so-called “Abstract Plasticism” generated paintings that seem as far removed from nature as they possibly could be (Taylor, 2002a, 2004). They consist of elements – primary colors and straight lines – that never occur in a pure form in the natural world. In contrast to Mondrian’s simplicity, Pollock’s “Abstract Expressionism” speaks of complexity – a tangled web of intricate paint splatters. Whereas Mondrian’s patterns are traditionally described as “artificial” and “geometric,” Pollock’s are “natural” and “organic” (Taylor, 2011). But if Pollock’s patterns celebrate nature’s organic shapes, what shapes would these be?

### Nature’s Fractals

Since the 1970s many of nature’s patterns have been shown to be fractal (Mandelbrot, 1982; Barnsley, 1993; Gouyet, 1996). In contrast to the smoothness of artificial lines, fractals consist of patterns that recur on finer and finer scales, building scale-invariant shapes of immense complexity. Even the most common fractal objects, such as the tree shown in Figure 1, contrast sharply with the simplicity of artificial shapes.

An important parameter for quantifying a fractal pattern’s visual complexity is the fractal dimension, D. This parameter describes how the patterns occurring at different magnifications combine to build the resulting fractal shape (Mandelbrot, 1982). For Euclidean shapes, dimension is described by familiar integer values – for a smooth line (containing no fractal structure) D has a value of 1, whilst for a completely filled area (again containing no fractal structure) its value is 2. However, the repeating patterns of a fractal line cause the line to begin to occupy space. As a consequence, its D value lies between 1 and 2. By increasing the amount of fine structure in the fractal mix of repeating patterns, the D value moves closer to 2 (Mandelbrot, 1982; Taylor and Sprott, 2008).

Thus, for fractals described by a low D value, the small content of fine structure builds a very smooth, sparse shape. However, for fractals with a D value closer to two, the larger content of fine
structure builds a shape full of intricate, detailed structure (Taylor and Sprott, 2008). Figure 2 (left column) demonstrates how a pattern’s $D$ value has a profound effect on the visual appearance. The pattern established by clouds (left, top) has a $D$ value of 1.3, while the pattern established by the trees (left, bottom) has a $D$ value of 1.9. Table 1 shows $D$ values for various natural forms.

**Pollock’s Fractals**

In 1999, we published an analysis of Pollock’s paintings that confirmed his poured patterns to be fractal (Taylor et al., 1999a). Building on this initial analysis, a number of groups have shown diverse fractal analysis techniques to be useful approaches to quantifying the visual complexity of Pollock’s poured patterns (Mureika et al., 2004, 2005; Mureika, 2005; Lee et al., 2006, 2007; Graham and Field, 2007, 2008; Redies, 2007; Redies et al., 2007; Alvarez-Ramirez et al., 2008a,b; Coddington et al., 2008; Irfan and Stork, 2009; Fairbanks et al., 2010). Our initial analysis employed the well-established “box-counting” method, in which digitized images of Pollock paintings were covered with a computer-generated mesh of identical squares (or “boxes”). The statistical scaling qualities of the pattern were then determined by calculating the proportion of squares occupied by the painted pattern and the proportion that were empty. This process was then repeated for meshes with increasingly small square sizes. Reducing the square size is equivalent to looking at the pattern at finer magnification. In this way, we could compare the pattern’s statistical qualities at different magnifications. Specifically, the number of squares, $N(L)$, that contained part of the painted pattern were counted and this was repeated as the size, $L$, of the squares in the mesh was reduced. The largest size of square was chosen to match the canvas size ($L \sim 2.5$ m) and the smallest was chosen to match the finest paint work ($L \sim 1$ mm). For fractal behavior, $N(L)$ scales according to the power law relationship $N(L) \sim L^{-\alpha}$,
where $1 < D < 2$. This power law generates the scale-invariant properties that are central to fractal geometry. The $D$ values, which chart this scale invariance, were extracted from the gradient of a graph of log $N/L$ plotted against log $L$. Details of the procedure, along with typical graphs, are presented elsewhere (Taylor et al., 2007). We note that the standard deviation associated with fitting the data to the fractal scaling behavior is such that $D$ can be determined to an accuracy of two decimal places (Taylor et al., 2007).

Many of Pollock’s paintings are composed of a number of distinctly colored paint layers. One of the central challenges is to separate these layers so that each can be passed through the box-counting analysis. Colors have been filtered using the “physical” model based on red–green–blue primaries (Taylor et al., 1999a, 2007; Mureika, 2005) and also a “perceptual” model based on L*a*b* color space (Mureika, 2005). The extracted patterns are labeled as color “blobs,” and light-colored blobs typically have higher $D$ values than darker blobs (Mureika, 2005). The question of how Pollock combined the blobs into an integrated, multi-colored visual fractal led us to investigate his painting technique in detail. We described Pollock’s style as “Fractal Expressionism” (Taylor et al., 1999b; Taylor, 2011) to distinguish it from computer-generated fractal art. Fractal Expressionism indicates an ability to generate and manipulate fractal patterns directly. In many ways, this ability to paint such complex patterns represents the limits of human capabilities. Our analysis of film footage taken at his peak in 1950 reveals a remarkably systematic process (Taylor et al., 2002). He started by painting localized islands of trajectories distributed across the canvas, followed by longer extended trajectories that joined the islands, gradually submerging them in a dense fractal web of paint. This process was very swift with the fractal dimension rising sharply to a mid-range value of $D = 1.5$ at 20 s. He would then break off and later return to the painting over a period of several days, depositing extra layers on top of this initial “anchor” layer (Taylor, 2011). Whether or not fractal layers merge to create a combined pattern that is also fractal depends on the relative $D$ values of the individual layers, their densities and their degrees of overlap (Taylor et al., 2006; Taylor, 2011). In Pollock’s painting process, the combined patterns are fractal (Taylor et al., 2002; Mureika, 2005). The dark-colored, anchor layer set the initial $D$ value of the painting, which was then fine-tuned by adding multiple, light-colored layers (Taylor et al., 2002). This fine-tuning process has been interpreted in terms of a mathematical union of the individual fractal layers (Vicsek, 1989), in which the combined pattern has a $D$ value that matches the highest $D$ of the individual layers (Mureika et al., 2005): thus as lighter-colored, higher $D$ layers were added, the painting’s overall $D$ value rose. Pollock’s multi-stage painting technique was therefore clearly aimed at generating high $D$ fractal paintings (Taylor, 2011).

As shown in Figure 3, he perfected this technique over 10 years. Art theorists categorize the evolution of Pollock’s pouring technique into three phases (Varndoe and Karmel, 1998). In the “preliminary” phase of 1943–1945, his initial efforts were characterized by low $D$ values. An example is the fractal pattern of the painting Untitled from 1945, which has a $D$ value of 1.10 (see Figure 2). During his “transitional phase” from 1945 to 1947, he started to experiment with the pouring technique and his $D$ values rose sharply (as indicated by the first gradient in Figure 3). In his “classic” period of 1948–1952, he perfected his technique and $D$ rose more gradually (second gradient in Figure 3) to the value of $D = 1.7$. During his classic period he also painted Untitled (see Figure 2), which has an even higher $D$ value of 1.89. However, he immediately erased this pattern (it was painted on glass), prompting the speculation that he regarded this painting as too complex and immediately scaled back to paintings with $D = 1.7$. This suggests that his 10 years of refining the pouring technique were motivated by a desire to generate fractal patterns with $D \sim 1.7$. This distinct evolution raises

<table>
<thead>
<tr>
<th>Natural pattern</th>
<th>Fractal dimension</th>
<th>Source</th>
</tr>
</thead>
<tbody>
<tr>
<td>Coastlines</td>
<td>1.05–1.52</td>
<td>Mandelbrot (1982), Feder (1988)</td>
</tr>
<tr>
<td>Galaxies (modeled)</td>
<td>1.23</td>
<td>Mandelbrot (1982)</td>
</tr>
<tr>
<td>Cracks in ductile materials</td>
<td>1.25</td>
<td>Louis et al. (1966)</td>
</tr>
<tr>
<td>Geothermal rock patterns</td>
<td>1.25–1.55</td>
<td>Cambel (1993)</td>
</tr>
<tr>
<td>Woody plants and trees</td>
<td>1.28–1.90</td>
<td>Morse et al. (1985)</td>
</tr>
<tr>
<td>Waves</td>
<td>1.3</td>
<td>Werner (1999)</td>
</tr>
<tr>
<td>Clouds</td>
<td>1.30–1.33</td>
<td>Lovejoy (1982)</td>
</tr>
<tr>
<td>Sea anemone</td>
<td>1.6</td>
<td>Burrough (1981)</td>
</tr>
<tr>
<td>Cracks in non-ductile materials</td>
<td>1.68</td>
<td>Skjeltorp (1988)</td>
</tr>
<tr>
<td>Snowflakes (modeled)</td>
<td>1.7</td>
<td>Nittmann and Stanley (1987)</td>
</tr>
<tr>
<td>Retinal blood vessels</td>
<td>1.7</td>
<td>Family et al. (1989)</td>
</tr>
<tr>
<td>Bacteria growth pattern</td>
<td>1.7</td>
<td>Matsushita and Fukiwara (1993)</td>
</tr>
<tr>
<td>Electrical discharges</td>
<td>1.75</td>
<td>Niemeyer et al. (1984)</td>
</tr>
<tr>
<td>Mineral patterns</td>
<td>1.78</td>
<td>Chopard et al. (1991)</td>
</tr>
</tbody>
</table>

Table 1 | $D$ values for various natural fractal patterns.
Taylor et al. Responses to Jackson Pollock’s fractals

The fractal dimension $D$ of Pollock paintings plotted against the year in which they were painted (1943–1953). See text for details. The right hand images show computer constructions of three of Pollock’s paintings.

FIGURE 3}

an intriguing question: did these higher $D$ fractal patterns hold a special esthetic quality for Pollock and, if so, do observers of his work share the same preference?

In the following sections, we will present our investigations of how observers look at Pollock’s fractals. Our initial motivation for extracting the box-counting dimension for Pollock’s patterns was to facilitate a direct comparison with previous investigations of human response to fractals, which focused on the relationship between their esthetic value and $D$ (see later). Before we move onto these comparisons, it is important to emphasize that $D$ is just one of a spectrum of dimensions that can be used to quantify the scaling properties of fractal patterns. A number of groups, including ours, have gained further insight into the rich structure of Pollock’s patterns by performing a multi-fractal analysis (Mureika et al., 2005; Coddington et al., 2008; Graham and Stork, 2009; Fairbanks et al., 2010). In addition, whereas our work focused on the colored blobs, the “edge” patterns extracted from the luminance gradients of grayscale images of Pollock’s work are also fractal (Mureika et al., 2005). The $D$ values extracted from these fractal edge patterns can be related mathematically to a power spectrum analysis of the grayscale images (Fairbanks and Taylor, 2011). Spectral analysis of Pollock’s paintings reveals a scale-invariant power law behavior (Redies et al., 2007; Alvarez-Ramirez et al., 2008a; Graham and Field, 2008). This latter result is appealing because it facilitates a comparison between the luminance properties of Pollock’s work and those of other artworks (Graham and Redies, 2010; Koch et al., 2010) and natural scenery (Switkes et al., 1978; Field and Brady, 1997; Ruderman, 1997; Billock, 2000; Billock et al., 2001). However, the relationship between the grayscale (i.e., power spectral analysis) and colored (i.e., box-counting analysis of the blobs) patterns of Pollock’s fractals is not without its complexities (Fairbanks and Taylor, 2011) and our future research will continue to seek a precise characterization of this relationship. For the remainder of the present article, we restrict our analyses to the blob $D$ values.

It is also valuable to highlight an inevitable restriction of all of the above forms of fractal analysis – that the fractal magnification range is limited. Unlike mathematical fractals, which span from the infinitesimally small through to the infinitely large, Pollock’s fractals can’t exceed the canvas size, nor can they be smaller than the smallest speck of paint. Concerns that Pollock’s limited magnification range prevents an accurate extraction of $D$ values have been successfully addressed elsewhere (Taylor et al., 2006; Taylor, 2011). Of more interest for the current study is whether this magnification range is sufficient for the fractals to induce marked responses in the human visual system. The results that follow show that a magnification factor of only 20 (i.e., the largest pattern is just 20 times larger than the smallest) is enough to trigger striking responses. Significantly, most of nature’s fractals match this highly limited magnification range and Pollock’s fractals exceed it.

**HOW DOES THE EYE SEARCH THROUGH THE VISUAL COMPLEXITY OF POLLOCK’S FRACTALS?**

The use of eye-tracking techniques to examine the gaze of the observer is a potentially powerful approach to understanding art appreciation (Busswell, 1935; Yarbus, 1967; Nodine and Krupinski, 2003; Locher, 2006). While eye-tracking investigations of many types of artworks have revealed a great inter individual variability in scan path characteristics, several systematic findings have emerged. For example, the spontaneous gaze behavior in viewing artworks seems to follow a “coarse-to-fine” strategy where an initial global sweep of the image is followed by a later period of visual scrutiny of finer local details (Locher et al., 2007). Furthermore, the points of high salience computed in terms of local feature differences in luminance, color and orientation were found to drive eye fixations in viewing abstract and representational artworks (Wallraven et al., 2007; DiPaola et al., 2010; Foulsham and Kingstone, 2010; Fuchs et al., 2011). Based on these investigations, how the eye scans across Pollock’s patterns, which lack obvious salient features and which scale across multiple sizes, is of obvious interest.

**Figure 4A** shows an eye-tracking system used in our study, which integrates infrared and visual camera techniques to determine the location of the eye’s gaze when looking at a pattern formed on a computer screen (Hyona et al., 2002). The sizes of the fractal images displayed on the screen were 290 by 290 mm, corresponding to 1024 by 1024 screen pixels (i.e., the image resolution was 35.3 pixels/cm). The eye-tracker can locate the gaze with an accuracy of 4 pixels.

**Figure 4B** shows a magnified section of the spatial pattern traced out by the eye’s gaze as it moves across the screen. As expected, the pattern is composed of long ballistic trajectories as the eye jumps between the locations of interest, and smaller motions called micro-saccades that occur during the dwell periods to ensure that the retina does not de-sensitize (Hyona et al., 2002). **Figure 4B** plots the horizontal ($x$) and vertical ($y$) locations in units of screen pixels. Micro-saccades are expected to occur over an angular range of typically $0.5^\circ$. This angle translates to a distance of 15 pixels on the screen and, as expected, this approximately matches the typical width of the dwell regions observed in **Figure 4B**.

**Figure 4C** shows the corresponding temporal pattern by plotting the $x$ position against time $t$. The periods of relative motionlessness are the dwell periods at a given location, during which time the eye is undergoing micro-saccades. The typical dwell time is approximately 0.4 s. The time scale of the individual micro-saccades is expected to be approximately 10–20 ms. We note that this is on...
observed fractal patterns. In each case, the \( D \) values of the saccades are averaged over the results from six observers, each of whom observed the nine fractal images for 30 s, separated by a checkerboard pattern observed for 30 s. The results confirm that the saccades trace out an inherent search pattern set at \( D = 1.5 \), regardless of the \( D \) values of the fractal pattern being observed (Fairbanks and Taylor, 2011).

This insensitivity to such a wide range of \( D \) values in the observed pattern is striking. It suggests that the eye’s search mechanism follows an intrinsic mid-range \( D \) value when in search mode. Why would the eye adopt a fractal trajectory with a \( D \) value of 1.5? An appealing possible answer lies in previous studies of the foraging behavior of animals. A number of successful investigations have proposed that animals adopt fractal motions when searching for food. See, for example, Viswanathan et al. (1996). Within this foraging model, the smaller trajectories allow the animal to look for food in small regions and then to travel to neighboring regions and then onto regions further away.

Significantly, such fractal motion has an “enhanced diffusion” compared to the equivalent random motion of Brownian motion. This might explain why it is adopted for both animal searches for food and the eye’s search for visual information. The amount of space covered by fractal trajectories is bigger than for random trajectories, and a mid-range \( D \) value appears to be optimal for covering terrain efficiently (Fairbanks and Taylor, 2011). The mathematical properties of fractals, therefore, provide the explanation for why the human eye follows a fractal trajectory with an inherent \( D \) value set at 1.5.

The same order as the sampling rate of the eye-tracking equipment (16 ms, 60 Hz). This measurement limitation would, therefore, impact on any studies of the micro-saccades. However, the focus of our investigations lies with the saccades, since these larger motions are the ones that dictate the search motion, and these operate on longer time scales than the equipment’s sampling rate.

**Figure 5** shows the eye’s spatial patterns (red trajectories) superimposed on Pollock’s fractal paintings that were displayed on the computer screen. The observer was instructed to memorize the observed painting in order to induce the search activity. The observation period lasted 60 s. The \( D \) values of the displayed monochrome paintings from left to right were 1.11, 1.66, and 1.89. The fourth image (right) is a Pollock painting composed of four differently colored interlocking fractal patterns, each with a \( D \) value of 1.6.

Details of the box-counting analysis applied to the eye spatial pattern can be found elsewhere (Fairbanks and Taylor, 2011). The results show that the eye trajectories trace out fractal patterns with \( D \) values that are insensitive to the \( D \) value of the fractal pattern being observed: the saccade pattern is quantified by \( D = 1.4 \), even though the underlying pattern varied over a very large range from 1.11 to 1.89. We note that this characteristic value of \( D = 1.4 \) also holds for observations of multi-colored fractals (far right image of Figure 5).

To test this result further, we considered another form of fractal pattern for observers to search through – the computer-generated fractals shown in **Figure 6**. **Table 2** compares the \( D \) values of the spatial patterns traced out by the saccades and the \( D \) values of the observed fractal patterns. In each case, the \( D \) values of the saccades are averaged over the results from six observers, each of whom observed the nine fractal images for 30 s, separated by a checkerboard pattern observed for 30 s. The results confirm that the saccades trace out an inherent search pattern set at \( D = 1.5 \), regardless of the \( D \) values of the fractal pattern being observed (Fairbanks and Taylor, 2011).

**Figure 4** shows the eye-tracking apparatus. Subsections of a single eye-tracking data set: the spatial pattern plotted in the \( x \) (horizontal) and \( y \) (vertical) directions, **(B)** and the time series \( x \) vs. time **(C)**.

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This model raises an intriguing question – what happens when the eye is made to view a fractal pattern of $D = 1.5$? Will this trigger a “resonance” when the eye sees a fractal pattern that matches its own inherent characteristics? Could such a resonance lead to a peak in esthetic appeal? In the next section, we will use visual perception experiments to explore this hypothesis.

THE ESTHETICS OF FRACTALS

The prevalence of fractals in our natural environment has motivated a number of studies to investigate the relationship between a pattern’s fractal character and its visual properties (Pentland, 1984; Cutting and Garvin, 1987; Jang and Rajala, 1990; Knill et al., 1990; Rogowitz and Vosset et al., 1990; Gilden et al., 1993; Geake and Landini, 1997). Whereas these studies concentrated on perceived qualities such as roughness and complexity, other studies have focused on esthetics and the quantification of the “visual appeal” of fractal patterns (Sprott, 1993; Pickover, 1995; Aks and Sprott, 1996; Taylor, 1998, 2001; Richards and Kerr, 1999; Richards, 2001; Spehar et al., 2003; Hagerhall et al., 2004; Taylor and Sprott, 2008; Boon et al., 2011). In one of the initial experiments performed in 1994, we used a chaotic pendulum called the “Pollockiser” to generate fractal and non-fractal poured paintings (example sections from two paintings are shown in Figure 7; Taylor, 2011). In the perception studies that followed, participants were shown one fractal and one non-fractal pattern (randomly selected from 40 images) and asked to state a preference (Taylor, 1998, 2003). Out of the 120 participants, 113 preferred examples of fractal patterns over non-fractal patterns, confirming their powerful esthetic appeal.

Given the profound effect that $D$ has on the visual appearance of fractals (see, for example, Figure 2), do observers base esthetic preference on the fractal pattern’s $D$ value? Previous studies by Aks and Sprott used computer-generated fractals and reported preferred values of 1.3 (Sprott, 1993; Aks and Sprott, 1996). To determine if this was a “universal” esthetic quality of fractals, we performed an experiment incorporating all three categories of fractal pattern: fractals formed by nature’s processes (natural scenery), by mathematics (computer-generated images) and by humans (Pollock paintings) (Spehar et al., 2003). Within each category of fractals (i.e., mathematical, natural, natural)

Table 2 | A comparison of the $D$ values of the fractal images being viewed, and the $D$ values of the patterns traced out by the saccades.

<table>
<thead>
<tr>
<th>$D_{image}$</th>
<th>$D_{saccade}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.1</td>
<td>1.5</td>
</tr>
<tr>
<td>1.2</td>
<td>1.5</td>
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<tr>
<td>1.3</td>
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<td>1.8</td>
<td>1.5</td>
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<tr>
<td>1.9</td>
<td>1.5</td>
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</table>
and human), we investigated the visual preference as a function of $D$. This was done using a “forced choice” paired comparison technique, in which participants were shown a pair of images with different $D$ values on a monitor and asked to choose the more “visually appealing.” Introduced by Cohn (1894), the forced choice paired comparison technique is well-established for securing value judgments. In our experiments, all the images were paired in all possible combinations. The presentation order was fully randomized and preference was quantified in terms of the proportion of times each image was chosen. The results, based on 220 participants, indicated that across all categories the visual preference peaks for fractal dimension between 1.3 and 1.5, whereas lower visual preferences are found for fractals outside of this range (Spehar et al., 2003).

We have further extended these findings by measuring visual preference for the same computer-generated fractals that were used in our eye-tracking experiments. The results of this new investigation are shown in Figure 8.

For each panel in Figure 8, we show how the visual preference for fractal patterns depends on their $D$ values. The four panels investigate the response to different fractal “configurations” created using the same computer generation process. The same 20 observers viewed each image configuration and the results reveal a remarkable consistency in terms of the preference across the different configurations. For each configuration of fractal image, visual preference was significantly affected by a pattern’s fractal dimension ($F_{8,19} = 22.16, p < 0.0001$). As in our previous study (Spehar et al., 2003), the highest average visual preference is observed for fractal dimensions in the 1.3–1.5 range. A comparison across the four panels shows how little this preference varies for different examples of fractal patterns with the same $D$ value. This “universal” character of fractal esthetics is further emphasized by an investigation indicating that gender and cultural background of participants did not significantly influence preference (Abraham et al., 2011).

The above perception experiments deliberately focused on relatively simple fractal objects. Each image featured just one form of fractal pattern (for example, the clouds or trees shown in Figure 2). Furthermore, the selected images provided a relatively high contrast against a uniform background, facilitating the application of the box-counting technique. An obvious step is to extend our studies to consider preferences for natural scenes, which typically feature a combination of several different fractal objects (e.g., clouds, tress, mountains etc). Although the characteristics of typical scenes are considerably more subtle than the simple shapes considered above, their fractal statistics are well-charted. Analysis has shown that typical scenes are scale invariant, following a power law behavior (Field and Brady, 1997; Billock, 2000; Billock et al., 2001). This behavior is thought to be due to a combination of the following factors: (i) many of the individual objects in the scene are fractal (see Table 1), (ii) many scenes contain a power law distribution of object sizes (Field and Brady, 1997; Ruderman, 1997), and (iii) the structure in each of the luminance edges in the scene is expected to follow a power law distribution of sizes (Switkes et al., 1978).

The experimental procedures were approved by the School of Psychology, the University of New South Wales Human Research Ethics Advisory Panel. Informed consent was obtained from all subjects.
Does the preference for mid-range $D$ values of simple fractal objects (Sprott, 1993; Aks and Sprott, 1996; Spehar et al., 2003) extend to these more visually intricate fractal scenes? One possible approach to addressing this issue would be to concentrate on the luminance properties of the overall scene. This could be done by adopting the technique that performs a spectral analysis of the spatial frequencies of the grayscale image of the scene, as discussed earlier (Field and Brady, 1997; Billock, 2000). The appeal of this approach is that the grayscale analysis can be related to key variables in studies of spatial vision, such as Michelson contrast. Furthermore, the grayscale image conveys visual information about the “textures” of a scene and previous fractals research indicates that roughness texture is an important property for perception – in particular, a strong correlation has been found between fractal dimension and perceived roughness (Pentland, 1984; Jang and Rajala, 1990). In contrast, other research indicates that perception is determined by the edge contours of the observed fractal pattern (Rogowitz and Voss, 1990). Therefore, an alternative approach to the analysis of a fractal scene would be to select a prominent edge contour and investigate its impact on perception. The importance of edge contours to the visual system is supported by eye-tracking experiments which show that, in free viewing situations, subjects fixate on definite contours (Rayner and Pollatsek, 1992). The dominant contour in many scenes is formed by the skyline, and consequently these contours have been the focus of previous perception studies. In particular, in architectural studies of tall building skylines, the silhouette complexity significantly affected preference scores while facade complexity was of less importance (Heath et al., 2000). Furthermore, perception experiments using computer-generated images have investigated the impact of matching a city skyline to the background horizon formed by fractal mountains (Stamps, 2002).

Due to this inter-disciplinary interest, our investigations of fractal scenery focused on the importance of the skyline contour for determining esthetic preference of natural scenes (Hagerhall et al., 2004). The skyline contour of natural scenes has previously been found to be fractal, with the $D$ value depending on the objects that define the contour (Keller et al., 1987). Our box-counting analysis of the skyline contours extracted from 80 scenes photographed in Australia, Sweden and Italy confirms this fractal behavior. The procedure for extracting the skyline contour, shown in Figure 9, is described in detail elsewhere (Hagerhall et al., 2004). The preference experiments, involving 119 participants from the general public, show the most preferred $D$ value to be 1.3 (Hagerhall et al., 2004), indicating that the preference for mid-range $D$ values revealed for simple fractal shapes (Aks and Sprott, 1996; Spehar et al., 2003) appears to extend to the fractal characteristics of more intricate fractal scenery. The preference for skyline contours with $D = 1.3$ was also confirmed in another study with 63 students in psychology and landscape architecture who rated 12 landscape silhouettes extracted from photographs of natural scenery. In addition to preference, the participants rated the “naturalness” of the silhouettes and the results showed that the perceived naturalness was also highest for the silhouettes with a fractal dimension of around 1.3 (Hagerhall, 2005).

To summarize this section, perception studies of fractals generated by nature, mathematics and art indicate that images in the range $D = 1.3–1.5$ have the highest esthetic appeal. These mid-$D$ values are close to the $D$ values of 1.4–1.5 values predicted from the eye-tracking experiments.

**NEUROPHYSIOLOGICAL RESPONSE TO FRACTALS**

Does this visual appreciation for mid-range $D$ values affect the physiological condition of the observer? In particular, do mid-$D$ fractals also induce relaxation in the observer? This question motivated us to analyze the results of experiments performed at the NASA-Ames Research Center, in which 24 participants were seated in a simulated space station cabin, each facing one image on the wall. During continuous exposure to the image, each participant performed a sequence of mental tasks designed to induce physiological stress. Each task period was separated by a 1-min recovery period, thus creating a sequence of alternating high and low stress periods. To measure the subject’s physiological response to the stress of mental work, skin conductance was monitored continuously during this sequence (Taylor, 2006). Prior studies have shown skin conductance to be a reliable indicator of mental performance stress with higher conductance occurring under high stress (Ulrich and Simons, 1986). The results showed that the mental tasks induced the smallest rise in stress when the observer was observing a fractal pattern with a $D$ value of 1.4 (Taylor, 2006).

**FIGURE 9** The processing steps used in the extraction of the fractal skyline contour of a natural scene. Top: one of the natural scenes shown to subjects. Middle: an intermediate processing step used to extract the skyline contour. Bottom: the extracted skyline contour subjected to the box-counting fractal analysis.
To build on this result, we extended our studies of relaxation to include neurophysiological responses (Hagerhall et al., 2008). This was done by monitoring subjects’ quantitative EEG (qEEG) response while viewing fractals with different $D$ values. Previous EEG recordings by others have shown that people are more wakefully relaxed during exposure to natural landscapes than during exposure to townscapes (Ulrich, 1981) and studies of wall art in hospitals find that images with natural content have positive effects on anxiety and stress (Ulrich, 1993). However, the definition of “nature” adopted in these previous studies was vague compared to our proposal of considering the $D$ dependence.

It is generally agreed upon that EEG is a good indicator of cortical arousal. Similarly, there seems to be agreement that, in the awake brain, power in the alpha-band (9–12 Hz) of the EEG is inversely related to activity (Laufs et al., 2003a,b; Oakes et al., 2004). Human behavior also seems to be more strongly related to the alpha-band than to the other frequency bands in the EEG (Davidson and Hugdahl, 1996) and that the alpha components seem to be especially responsive to environmental stimulation (Küller, 1991; Küller et al., 2009). While the alpha component of EEG is considered to show a wakefully relaxed state, the delta component (2.25–3 Hz) is prominent during drowsiness and deep sleep. The beta component (18–24 Hz) is associated with external focus, attention and an alert state (Kolb and Whishaw, 2003). Three regions of the brain—frontal, parietal and temporal—were chosen for the qEEG recordings. Processes in these three associational zones are thought to be complementary (Kolb and Whishaw, 2003). Hence, the three selected regions are expected to reveal significant psycho-physiological impacts of exposure to fractal images.

Based on the preferences for mid-$D$ fractals and the possibility, based on the skin conductance measurements, that these fractals might also induce a relaxed state (Taylor, 2006), we hypothesized that mid-$D$ fractals would produce a maximal alpha response in the frontal areas. Additionally, we hypothesized that the different fractal dimensions would generate different levels of activation in the processing of the pattern, i.e., a difference in beta responses would be likely in the parietal and temporal regions.

Computer-generated fractal skylines, shown in Figure 10, were chosen with the $D$ values of 1.14, 1.32, 1.51, and 1.70. Thirty-two subjects participated in the study. The fractal images were viewed for 1 min each and interspaced by a neutral gray picture for 30 s. This exposure period was chosen to ensure that a relaxation effect in the subjects could occur. Half of the subjects viewed the stimuli with increasing fractal dimension and the other half with decreasing fractal dimension. During the viewing, qEEG was continuously monitored and recorded using a digital EEG recorder.

The results shown in Figure 11 indicate that fractal images quantified by $D = 1.3$ induce the largest changes in subjects’ qEEG response (Hagerhall et al., 2008). This supports the proposal emerging from perception studies that these patterns are visually unique. These fractals generated the maximal alpha response in the frontal region, consistent with the hypothesis that they are most relaxing. They, at the same time, generated the highest beta response in the parietal region, indicating that this pattern was conversely generating most activation in the processing of the pattern’s spatial properties. This points to a very interesting interplay between these brain areas for mid-$D$ fractals, which requires further investigation.

Current studies are using the fMRI technique to identify more precisely the regions of the brain that are preferentially activated when observing the stress-reducing fractals. Preliminary results suggest that mid-$D$ fractals activate the ventral visual stream (including the ventrolateral temporal cortex), the parahippocampal region, and the dorsolateral parietal cortex, involved with spatial long-term memory.

![Figure 10](image-url) **Figure 10** | The fractal skylines used in the qEEG study. The fractal dimensions of the images were as follows: $D$ (A) 1.14 (B) 1.32 (C) 1.51 and (D) 1.70.
**CONCLUSION**

Scientific experiments might appear to be a highly unusual tool for judging art. However, our preliminary experiments provide a fascinating insight into the impact that art might have on the perceptual, physiological and neurological condition of the observer. Our future investigations will explore the possibility of incorporating

Interestingly, the parahippocampal area has also been discussed in relation to detection and regulation of emotional input, for instance with reactions to happy and sad classical music (Mitterschiffthaler et al., 2007). These studies belong to the emerging field of “neuro-aesthetics,” which explores the relationship between the neural cells activated and the esthetics of the object being observed (Zeki, 1999).

![Significant effects of the fractal dimension D on EEG.](image)

**FIGURE 11 | Significant effects of the fractal dimension D on EEG.** Mean and SD in mV² (Mean ± SD). Error bars represent 95% confidence intervals. (A) Alpha for frontal regions F3F4 together for D = 1.14 (2.28 ± 1.77), D = 1.32 (2.80 ± 2.36), D = 1.51 (2.53 ± 2.09), and D = 1.70 (2.39 ± 1.88). (B) Delta for the frontal regions F3F4 together for D = 1.14 (5.57 ± 5.96), D = 1.32 (4.91 ± 4.44), D = 1.51 (6.06 ± 6.11), and D = 1.70 (5.60 ± 5.86). (C) Beta for the parietal regions P3P4 together for D = 1.14 (1.69 ± 1.57), D = 1.32 (1.95 ± 1.74), D = 1.51 (1.80 ± 1.63) and D = 1.70 (1.76 ± 1.54).
fractal art into the interior and exterior of buildings, in order to adapt the visual characteristics of artificial environments to the positive responses.


Is Jackson Pollock an artistic enigma? According to our results, the low $D$ patterns painted in his earlier years should have more “visual appeal” than the higher $D$ patterns in his later classic poured paintings. What was motivating Pollock to paint high $D$ fractals? Should we conclude that he wanted his work to be esthetically challenging to the gallery audience? It is interesting to speculate that Pollock might have regarded the visually restful experience of a low $D$ pattern as being too bland for an artwork and that he wanted to keep the viewer alert by engaging their eyes in a constant search through the dense structure of a high $D$ pattern. Speculation over Pollock’s preference for high $D$ fractals leads us back to the fundamental question driving this article: why do most people prefer fractals in the range $D = 1.3–1.5$?

We have noted that one potential explanation lies in a “resonance” with our eye trajectories, which trace out fractal patterns characterized by $D = 1.4–1.5$ when in search mode. However, an alternative explanation was presented by Aks and Sprott (1996) when interpreting their pioneering perception experiment. They speculated that the preference for mid-range $D$ values is set through exposure to nature’s fractal patterns. Indeed, Table 2 shows that many of nature’s fractals cluster around $D = 1.3$. Perhaps then people’s preference for mid-range fractals is based on familiarity with these $D = 1.3$ shapes! Intriguingly, Table 2 also reveals another cluster at $D = 1.7$, matching Pollock’s preference, raising the possibility that Pollock’s preference was set by exposure to these more complex fractals (Taylor, 2011).

Others have used traditional theories of esthetics to explain Pollock’s preference. For example, Mureika appealed to the peak shift effect (Mureika, 2005), one of the “eight laws of artistic experience” (Ramaschandran and Hirstein, 1999). Within this esthetics model, visual interest is strengthened by overtly enhancing key characteristics of an image, in Pollock’s case the $D$ value. Another esthetics model, the “principle of the esthetic middle,” predicts that the viewer will be drawn to a visual scene of mid-complexity (Berlyne, 1971). Given that higher $D$ values exhibit higher visual complexity through their higher content of fine structure (Sprott and Taylor, 2008), this might explain why most people prefer mid-$D$ fractals, but not Pollock’s quest for higher values. Recent studies that supplement $D$ with other measures of complexity, such as $G_2$ file size and algorithm length (Taylor and Sprott, 2008; Boon et al., 2011; Forsythe et al., 2011), might prove useful in addressing this issue.

The discrepancy between Pollock’s preference and those of other observers might also lie in the fact that the paintings might have looked different to Pollock simply because he spent so much time generating and looking at them. Webster has argued that a prolonged exposure to any pattern or a visual environment leads to a process of adaptation, a process through which the perceptual norms are constantly adjusted (Webster, 2002). We plan to test the idea of habituation to fractals in future experiments that examine if exposure to high $D$ fractals causes the observer’s preference to move to these higher $D$ values.

We finish with a remark made by one of Pollock’s friends, Ruebin Kadish, who noted, “I think that one of the most important things about Pollock’s work is that it isn’t so much what you’re looking at but it’s what is happening to you as you’re looking at his particular work” (Bragg, 1987). This observation emphasizes both the importance of the long tradition of experimental esthetics (Fechner, 1876) and the value of employing modern tools for analyzing human response to art works.

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