Political Economy - The Economic Origins of Democracy

February 25, 2013

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 - Why did some societies evolve into democracies relatively peacefully and others violently?
 - Why do some democracies appear secure whereas other are quite fragile?

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 - It must therefore be the case that if they do so it is because others are able to undertake actions that benefit the oligarchs more than those which they themselves could carry out
 - Thus to delegate decision making power to others is rational

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 - $C(\tau)$ is increasing and convex, so $C'(\tau) > 0$ and $C''(\tau) > 0$
 - Each agent receives a transfer T

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$$T = \frac{\tau(Ry_r + Py_p) - C(\tau)(Ry_r + Py_p)}{N}$$
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• The indirect utility functions of rich and poor

$$V(y_r|\tau) = (1-\tau)y_r + (\tau - C(\tau))\bar{y}$$

$$V(y_p|\tau) = (1-\tau)y_p + (\tau - C(\tau))\bar{y}$$

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Implicit solutions

$$\begin{split} &C'(\tau_r{}^*) = \frac{\bar{y} - y_r}{\bar{y}} = 1 - \rho_r \\ &C'(\tau_\rho{}^*) = \frac{\bar{y} - y_\rho}{\bar{y}} = 1 - \rho_\rho \end{split}$$

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• Given $C(\tau)$ is increasing and convex $\tau_p^* > \tau_r^* \Rightarrow$ the poor prefer higher tax rates than the rich \Rightarrow Redistributive conflict

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 - \bullet A revolution is costly μ of all incomes are destroyed in perpetuity by the conflict
 - No revolution constraint (NRC)

$$V(y_p, \mu|{\tau_p}^*) \leq V(y_p|{\tau_r})$$

$$\Rightarrow (1 - \mu)((1 - \tau_{p}^{*})y_{p} + (\tau_{p}^{*} - C(\tau_{p}^{*}))\bar{y})$$

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$$V(y_{\rho}, \mu | \tau_{\rho}^*) \leq V(y_{\rho} | \tau_r)$$

$$\Rightarrow 0 \leq (1 - \tau_r)y_{\rho} + (\tau_r - C(\tau_r))\bar{y}$$

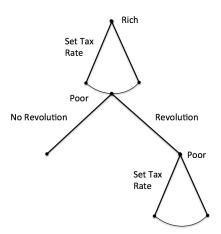
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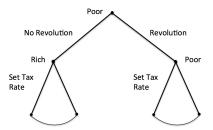
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No revolution and no democracy!

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There is never a revolution or democracy

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 - Every period in the models above is the same, so anything that holds in one period holds forever

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 - ullet When $\mu=1$ the rich are under no threat and will abandon the tax which if maintained forever would satisfy the NRC
 - The rich cannot credibly promise a tax rate that will satisfy the NRC and this is known by the poor. This is the commitment problem

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 - Strategic delegation solves the commitment problem

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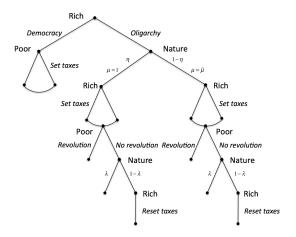
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 - The poor then choose revolution or not
 - If the poor choose revolution they then set taxes
 - If the poor do not choose revolution nature then chooses whether or not to let the rich reset taxes (Acemoglu's trick)

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ullet $\mu=1$ with probability λ , $\mu=ar{\mu}$ with probability $1-\lambda$

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 Revolutions and Commitment Problems - Peaceful Transition to Democracy

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 - If the NRC constraint fails when $\mu=\bar{\mu}$ then the rich will choose democracy if

$$\begin{split} (1 - \tau_{p}^{*}) y_{r} + (\tau_{p}^{*} - C(\tau_{r}^{*})) \bar{y} \\ & \geq \eta [(1 - \tau_{r}^{*}) y_{r} + (\tau_{r}^{*} - C(\tau_{r}^{*})) \bar{y}] \\ & + (1 - \eta) (1 - \bar{\mu}) [(1 - \tau_{p}^{*}) y_{r} + (\tau_{p}^{*} - C(\tau_{p}^{*})) \bar{y}] \end{split}$$

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