

Political Economy - Political Agency

January 29, 2013

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 - Moral hazard - unobservable action
 - Politicians actions may not be perfectly observable
 - Voters may not be able to perfectly deduce the actions that politicians took, but they can often observe something of the results

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 - Two time periods $t \in \{1, 2\}$

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⇒ **Moral Hazard**

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 ⇒ **Moral Hazard**
- Politicians type only observed by the incumbent politician
 ⇒ **Adverse Selection**

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 - All politicians experience an "ego-rent" of E
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 - Share voters objectives - always choose $e_t = s_t$
 - So payoff is $E + \Delta$

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 - Assume $R > \beta(\mu + E)$ - guarantees that dissonant politicians do **not** do what voters want some of the time

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 - Receive $E + r_t$ in t
 - Assume $R > \beta(\mu + E)$ - guarantees that dissonant politicians do **not** do what voters want some of the time
 - Let $e_t(s, i)$ with $s \in \{0, 1\}$ and $i \in \{c, d\}$ denote the politicians action in t

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 - Incumbent politician plays second and chooses
 - Action $e_1 \in \{0, 1\}$ - *observed only by politician*
 - Voters play last observe their payoffs and choose either
 - To reelect the incumbent politician
 - Replace the incumbent with random draw from the pool

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 - Action $e_2 \in \{0, 1\}$
 - All agents realize their payoffs

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 - Type of politician - i_2 - if they are replaced
 - Dissonance rent - r_2
 - Incumbent politician plays second and chooses
 - Action $e_2 \in \{0, 1\}$
 - All agents realize their payoffs
 - Game ends at the end of period 2

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 - All politicians behave optimally given the reelection rule of voters

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 - All politicians behave optimally given the reelection rule of voters
 - Voters use Bayes Rule to update their beliefs

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- Bayes Rule
 - The probability that two events a and c occur together may be written
 - $p(a|c)p(c)$ or $p(c|a)p(a) \implies p(a|c)p(c) = p(c|a)p(a)$

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- Bayes Rule
 - The probability that two events a and c occur together may be written
 - $p(a|c)p(c)$ or $p(c|a)p(a) \implies p(a|c)p(c) = p(c|a)p(a)$
 - Rearranging $p(a|c) = \frac{p(c|a)p(a)}{p(c)}$

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 - Now suppose c can also occur with b so
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 - $p(a|c) = \frac{p(c|a)p(a)}{p(c|a)p(a) + p(c|b)p(b)}$
 - Employing Bayes rule will allow the voters to make their best guess of a politicians type given their observations

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 - All agents in the model can work this out

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 - λ - probability dissonant politician does what voters want in period 1 - **Political Discipline**

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 - Applying Bayes Rule if Δ is observed gives

$$\begin{aligned} p(c|\Delta) &= \frac{p(\Delta|c)p(c)}{p(\Delta|c)p(c) + p(\Delta|d)p(d)} \\ &= \frac{\pi}{\pi + \lambda(1 - \pi)} = \Pi \geq \pi \end{aligned}$$

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- Dissonant politicians choice
 - Will choose $e_1(s, d) = s_1$ if

$$\begin{aligned} E + r_1 &\leq E + \beta(\mu + E) \\ \implies r_1 &\leq \beta(\mu + E) \end{aligned}$$

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$$\begin{aligned} E + r_1 &\leq E + \beta(\mu + E) \\ \implies r_1 &\leq \beta(\mu + E) \end{aligned}$$

- Probability of which (**political discipline**) is

$$\lambda = G(\beta(\mu + E))$$

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 - Dissonant politicians set $e_1 = s_1$ if $r_1 \leq \beta(\mu + E)$ which occurs with probability λ

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 - Dissonant politicians set $e_1 = s_1$ if $r_1 \leq \beta(\mu + E)$ which occurs with probability λ
 - Dissonant politicians set $e_1 = 1 - s_1$ if $r_1 > \beta(\mu + E)$ which occurs with probability $1 - \lambda$

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 - In the Perfect Bayesian Equilibrium
 - Congruent politicians always set $e = s$
 - Dissonant politicians set $e_2 = 1 - s_2$
 - Dissonant politicians set $e_1 = s_1$ if $r_1 \leq \beta(\mu + E)$ which occurs with probability λ
 - Dissonant politicians set $e_1 = 1 - s_1$ if $r_1 > \beta(\mu + E)$ which occurs with probability $1 - \lambda$
 - All politicians that choose $e_1 = s_1$ are reelected, those that do not are replaced

Political Agency

- Quality of Government

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 - Voters Expected Payoffs

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 - Period 1

$$V_1(\lambda) = [\pi + (1 - \pi)\lambda]\Delta$$

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$$V_1(\lambda) = [\pi + (1 - \pi)\lambda]\Delta$$

- Period 2

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$$V_1(\lambda) = [\pi + (1 - \pi)\lambda]\Delta$$

- Period 2

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- Discounted Voter Welfare

$$\begin{aligned} W(\lambda) &= V_1(\lambda) + \beta V_2(\lambda) \\ &= [\pi + (1 - \pi)\lambda]\Delta + \beta\pi[1 + (1 - \pi)(1 - \lambda)]\Delta \end{aligned}$$

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so
$$W_\lambda = (1 - \pi)(1 - \beta\pi)\Delta > 0$$

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$$\lambda = G(\beta(\mu + E))$$

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- So by substitution

$$\begin{aligned} W(\pi, \mu, \beta, E) = & [\pi + (1 - \pi)G(\beta(\mu + E))]\Delta \\ & + \beta\pi[1 + (1 - \pi)(1 - G(\beta(\mu + E)))]\Delta \end{aligned}$$

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- Change in the Discount Rate - β

$$W_{\beta}(\pi, \mu, \beta, E) = \{G'(\cdot)(\mu + E)[1 - \pi - \beta\pi] + [\pi + (1 - \pi)G(\beta(\mu + E))]\}\Delta$$

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 - If π small - dissonant politicians are proportionately greater in number, therefore their good behavior is more valuable to voters
 - If π is small we are less likely to replace a dissonant with a congruent in the second period so we are less concerned with detecting them and voting them out of office in period 1

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- Change in the Dissonant Politician's Payoffs - $\mu + E$

$$\begin{aligned} W_{\mu}(\pi, \mu, \beta, E) &= W_E(\pi, \mu, \beta, E) \\ &= (1 - \pi)\beta G'(\beta(\mu + E))[1 - \beta\pi] > 0 \end{aligned}$$

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- Change in the Proportion of Congruent Politicians - π

$$W_{\pi}(\pi, \mu, \beta, E) = \{(1 - G(\beta(\mu + E)) + \beta[1 + (1 - G(\beta(\mu + E))][1 - 2\pi])\}\Delta > 0$$

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- Raises voter welfare
 - More likely to get a congruent politician in period 1
 - More likely to get a congruent politician in period 2 to replace a dissonant politician that is not reelected

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Political Agency

- Quality of Government
 - Term Limits

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 - Suppose politicians are term limited to one period in office

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Political Agency

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 - Suppose politicians are term limited to one period in office
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 - No political discipline $\lambda = 0$
 - Dissonant politicians always choose $e_1(s, d) = (1 - s_1)$
 - Reduces voter welfare